## HW 12

For Problems 1-2, suppose RV $X$ has one of the following distributions (either $H_{0}$ or $H_{A}$ ):

| $X$ | $H_{0}$ | $H_{A}$ |
| :--- | :--- | :--- |
| $x_{1}$ | 0.2 | 0.1 |
| $x_{2}$ | 0.3 | 0.4 |
| $x_{3}$ | 0.3 | 0.1 |
| $x_{4}$ | 0.2 | 0.4 |

Problem 1 (9.4) Compute the likelihood ratio, $\Lambda$, for each possible value of $X$ and order the $x_{i}$ according to $\Lambda$.

Problem 2 (9.4) What is the likelihood ratio test rejection rule for $H_{0}$ vs $H_{A}$ at level $\alpha=0.2$ ? What is the test rejection rule at level $\alpha=0.5$ ?

Problem 3 (9.5) Determine if each of the following statements about (frequentist) hypothesis testing is true or false. Give a brief explanation as to why. Answers without an explanation will not receive full credit.
(a) A type I error occurs when the test statistic falls in the rejection region of the test.
(b) A type II error is more serious than a type I error.
(c) The power of a test is determined by the null distribution of the test statistic.
(d) The likelihood ratio is a random variable.

