## Quiz 2

Stat 61

## Due to Gradescope by 12:00AM Oct 4

1. Indicate which of the following statements about Bayesian estimation are FALSE. On another sheet of paper, provide a corrected version of the FALSE statements.
(a) If two studies produce different Bayesian point estimators, then at least one of the studies has made a mistake.
(b) If we find a $90 \%$ highest posterior density credible interval for a parameter $\theta$ to be $[0.51$, 2.20], then we are asserting that there is a $90 \%$ chance that $\theta$ is between 0.51 and 2.20 .
(c) A prior in Bayes' theorem is a marginal distribution.
(d) A credible interval is always symmetric about the posterior mode.

Consider the following estimators for $\theta$ based on a sample of $X_{1}, \ldots, X_{n}$ IID random variables that follow a $\operatorname{Gamma}(4, \theta)$ distribution with density $f(x ; \theta)=\frac{\theta^{4}}{6} x^{3} e^{-\theta x} I\{x \geq 0\}$.

$$
\hat{\theta}_{1}=\frac{3}{n} \sum_{i=1}^{n} \frac{1}{X_{i}} \quad \hat{\theta}_{2}=E\left[\hat{\theta}_{1} \mid \sum_{i=1}^{n} X_{i}\right] \quad \hat{\theta}_{3}=\frac{4 n}{\sum_{i=1}^{n} X_{i}}
$$

2. Which of the estimators above are functions of a sufficient statistic for $\theta$ ?
3. For a small sample, say of size $n=4$, which of the estimators above has the smallest mean squared error?
4. For an incredibly large sample, say of size $n>10,000$, which of the estimators above has the smallest mean squared error?

## Submitting instructions

Upload a scanned, completed version of this page to Gradescope by the deadline. You should also upload additional pages that show your work as scanned PDFs. Any additional pages must be clearly labeled and display how you arrived at the answers on this page. You will not receive full credit for handing in solutions without any work or justification.

